

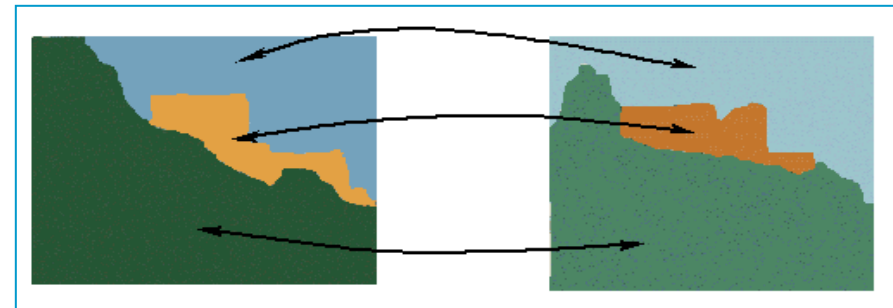
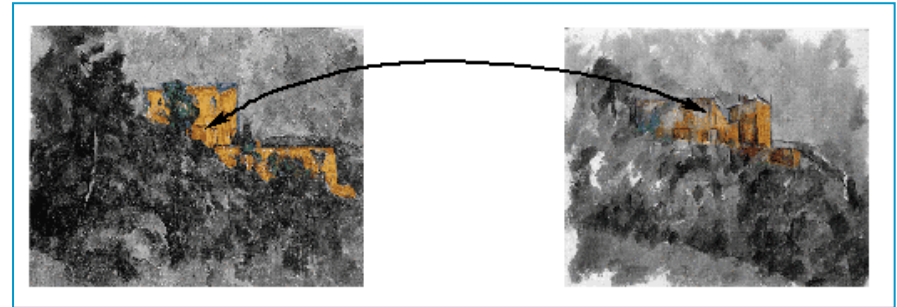
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# Retrieval of 2D Images by Spatial Arrangement of Color Clusters

University of Florence (UNIFI-MICC), Italy

# Spatial similarity in retrieval by content

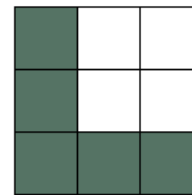
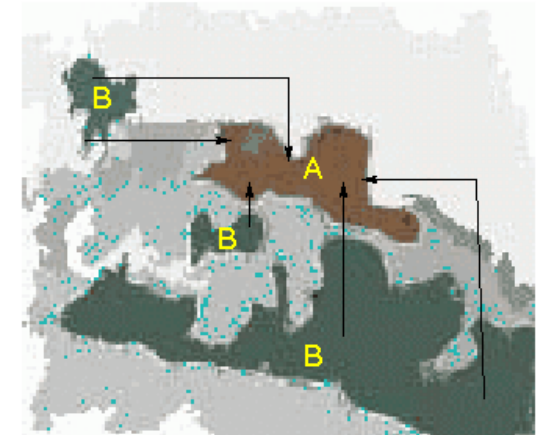
- Retrieval by visual content relies on appearing features of spatial entities
  - shape, color, texture, semantics
- When multiple entities are considered, the model may also capture relational information
  - spatial relationships



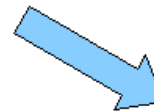
- This improves perceptual effectiveness
- But, basically changes the complexity of match and the applicability of indexing schemes

# Weighted walkthroughs between extended sets

- Cartesian reference system
- 9 walkthroughs  $w_{ij}$  along primitive directions, connecting pixels in A and B



- Each walkthrough is weighted with an integral measure of the number of pixel pairs to which it applies



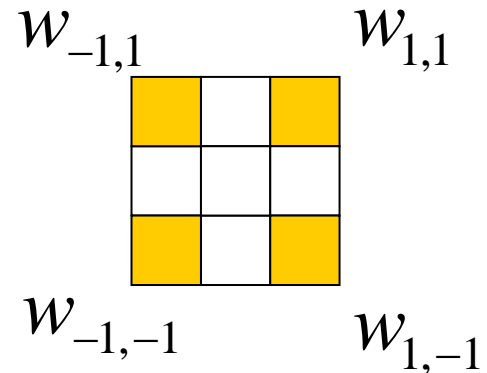
0.3	0	0
0.1	0	0
0.7	0.8	1

$ww(A,B)$

$$w_{ij}(A, B) = K_{ij} \int_A \int_B C_i(x_b - x_a) C_j(y_b - y_a) dx_b dy_b dx_a dy_b$$

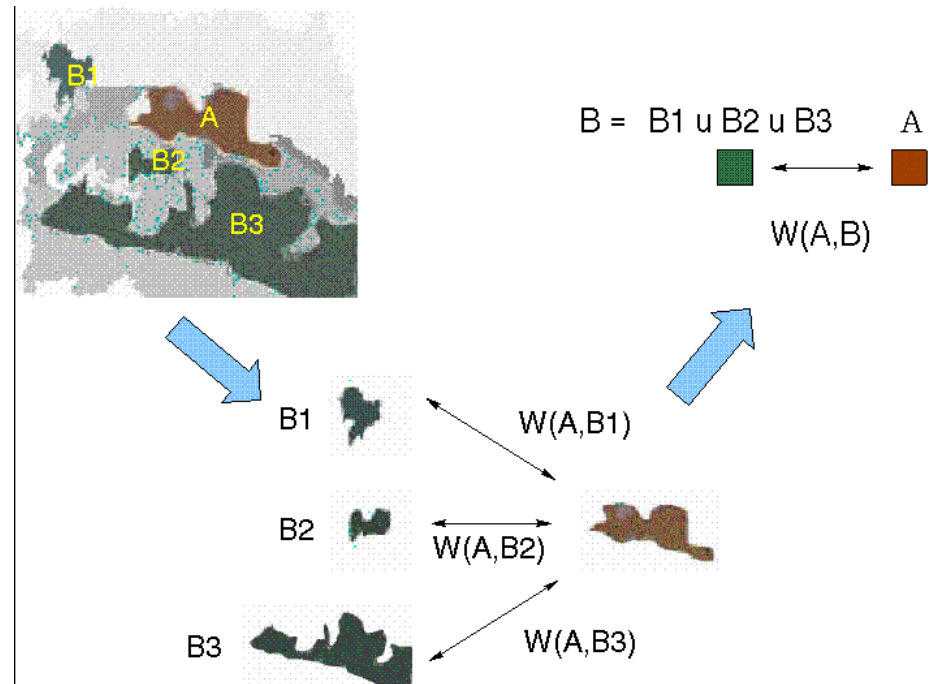
# Reduced set of weighted walkthroughs

- Weighted walkthroughs are simplified by considering only corner weights
  - evaluation of corner weights is as complex as a conventional representation based on centroids
  - avoids management of bounded rectangles requested by middle weights
  - neglects the central weight which is significant only when overlapping is considered



# Properties

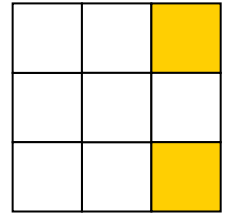
- Reflexive and invariant with respect to shifting and zooming
- Continuous with respect to changes in the image
- Compositional
  - the weight  $W(A, B_1 \cup B_2)$  is derived by linear combination of  $W(A, B_1)$  and  $W(A, B_2)$
- circumvents the complexity of numerical integration



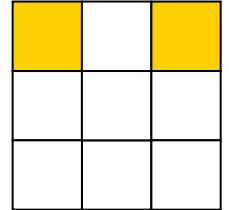
## Independent directional indexes

- The 4 corner have sum equal to 1 and can be replaced with 3 independent indexes

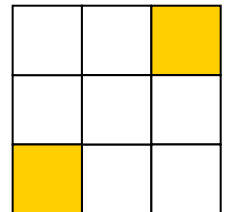
- $w_H(A, B) = w_{1,1}(A, B) + w_{1,-1}(A, B)$   
accounts for the degree by which  $A$  is on the left of  $B$



- $w_V(A, B) = w_{-1,1}(A, B) + w_{1,1}(A, B)$   
accounts for the degree by which  $A$  is below of  $B$

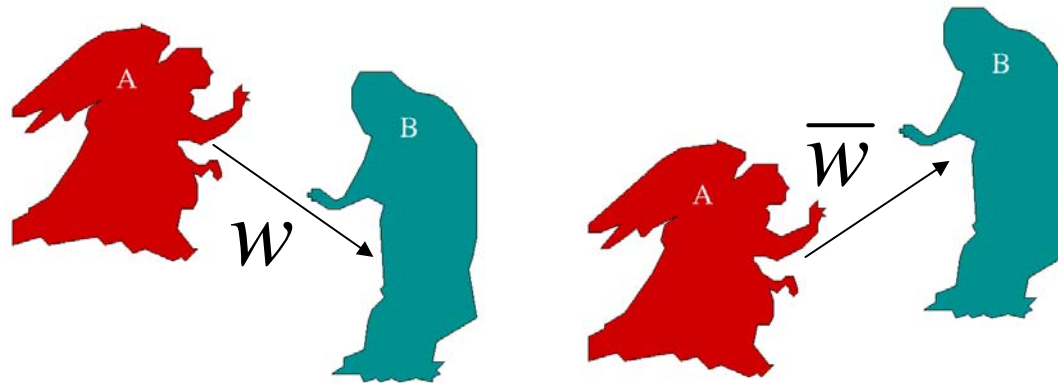


- $w_D(A, B) = w_{-1,-1}(A, B) + w_{1,1}(A, B)$   
accounts for the degree by which  $A$  and  $B$  are diagonal



## Distance measure

- Dissimilarity between spatial relationships is evaluated by convex composition of distances between homologous directional indexes



$$D(w, \bar{w}) = \alpha |w_H - \bar{w}_H| + \beta |w_V - \bar{w}_V| + \gamma |w_D - \bar{w}_D|$$

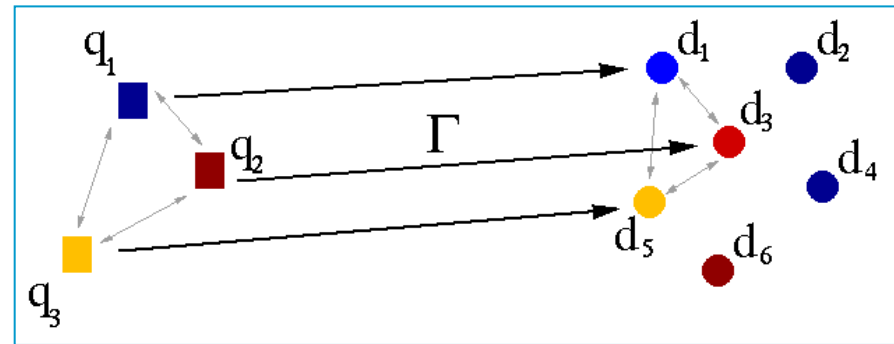
$$\alpha + \beta + \gamma = 1 \quad \alpha, \beta, \gamma \geq 0$$

- $D$  is a metric and changes with continuity

# Computing distances between graphs

- Comparison involves interpretation of the entities of a query on the entities of a description  $\Gamma : Q \rightarrow D$

- query specification  $\langle Q, a^q, s^q \rangle$
- image description  $\langle D, a^d, s^d \rangle$
- Interpretation  $\Gamma$  of  $Q$  on  $D$
- $q_1 \neq q_2 \rightarrow \Gamma(q_1) \neq \Gamma(q_2)$



- Distance under interpretation  $\Gamma:Q \rightarrow D$

- convex combination of distance between associated entities and between their homologous relationships

$$\mu(\Gamma) = \lambda\mu_s(\Gamma) + (1-\lambda)\mu_a(\Gamma)$$

$$\mu_a(\Gamma) = \sum_{k=1}^{N_Q} D_a(q_k, \Gamma(q_k))$$

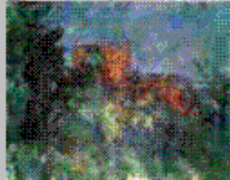
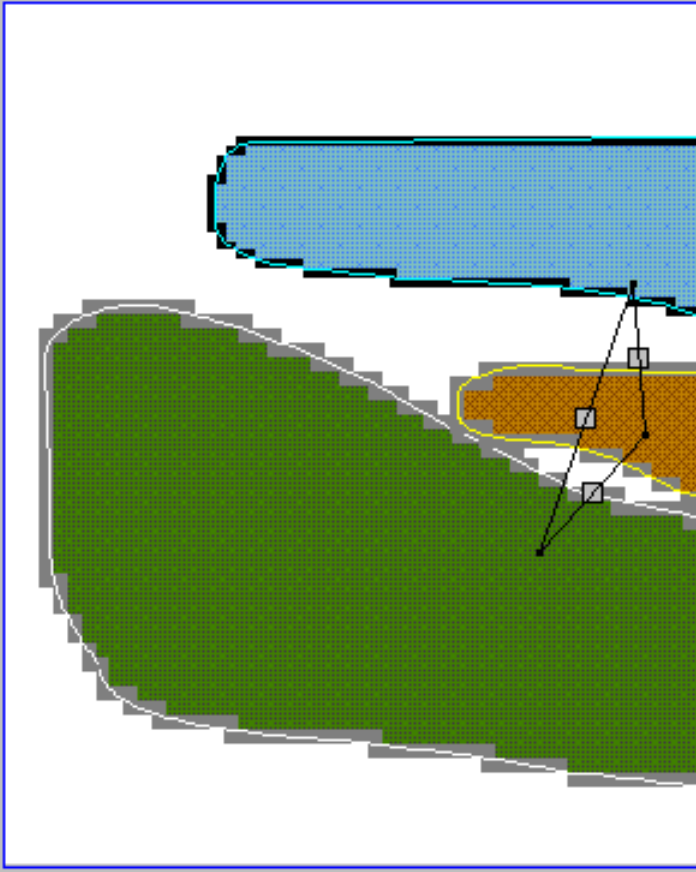
$$\mu_s(\Gamma) = \sum_{k=1}^{N_Q} \sum_{h=1}^{k-1} D_s(\langle q_k, q_h \rangle, \langle \Gamma(q_k), \Gamma(q_h) \rangle)$$

- The absolute distance is evaluated with the optimal interpretation

$$\mu = \text{Min}_{\Gamma:Q \rightarrow D} \{ \mu(\Gamma) \}$$

- The evaluation of a distance between two image models is an optimal error correcting (sub-)graph isomorphism problem





Distp: 0.000000



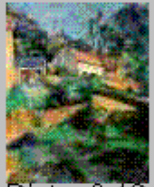
Distp: 0.105313



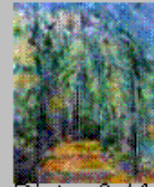
Distp: 0.110418



Distp: 0.116781



Distp: 0.12



Distp: 0.14



Distp: 0.149606



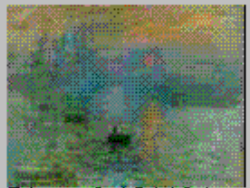
Distp: 0.157675



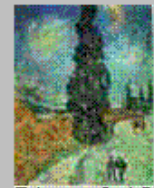
Distp: 0.160644



Distp: 0.160784



Distp: 0.161181



Distp: 0.16



Distp: 0.162150



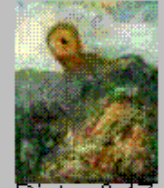
Distp: 0.163713



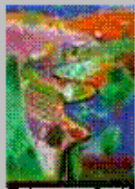
Distp: 0.165655



Distp: 0.168286



Distp: 0.17



Distp: 0.1



Distp: 0.171655



Distp: 0.172131

Dismiss

Object